

Foundations of Math 11

D. 368 # 1-6, 11(i, ii)

1. a) equation of the axis of symmetry is the vertical line that goes through the vertex

$$x = 4$$

- b) vertex is lowest or highest point on the parabola
 $(4, -16)$

- c) The domain of all quadratic functions is the same
 $\{x | x \in \mathbb{R}\}$

The range is all the points above or below the vertex.
 $\{y | y \geq -16, y \in \mathbb{R}\}$

2. a) $f(x) = 2x^2 + 8x + 8$
 y-intercept $(0, 8)$

to find a point on the graph,
 select a value to replace x
 in the equation and solve to
 find y

$$\begin{aligned} f(3) &= 2 \cdot 3^2 + 8 \cdot 3 + 8 \\ f(3) &= 18 + 24 + 8 \\ f(3) &= 50 \\ \text{point: } &(3, 50) \end{aligned}$$

$$\begin{aligned} f(-1) &= 2(-1)^2 + 8(-1) + 8 \\ f(-1) &= 2 - 8 + 8 \\ f(-1) &= 2 \end{aligned}$$

point: $(-1, 2)$

b) $f(x) = 4x - x^2$
 y-intercept $(0, 0)$

there is no constant
 so the y-intercept is 0

$$\begin{aligned} f(2) &= 4 \cdot 2 - 2^2 \\ f(2) &= 8 - 4 \\ f(2) &= 4 \\ \text{point: } &(2, 4) \end{aligned}$$

$$\begin{aligned} f(-3) &= 4(-3) - (-3)^2 \\ f(-3) &= -12 - 9 \\ f(-3) &= -21 \\ \text{point: } &(-3, -21) \end{aligned}$$

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3. x -intercepts \rightarrow where parabola crosses x -axis
 y -intercepts \rightarrow where parabola crosses y -axis
equation of axis of symmetry \rightarrow always a vertical line so always $x = \boxed{\quad}$
vertex \rightarrow the highest or lowest point on a parabola
domain \rightarrow all possible x -values for the parabola
range \rightarrow all possible y -values for the parabola

	(a)	(b)
x -int	0, 2	-1, 6
y -int	0	4
ax of sym	$x = 1$	$x = 2.5$
vertex	$(1, -2)$	$(2.5, 9.2)$
domain	$\{x x \in \mathbb{R}\}$	$\{x x \in \mathbb{R}\}$
range	$\{y y \geq -2, y \in \mathbb{R}\}$	$\{y y \leq 9.2, y \in \mathbb{R}\}$

	(a)	(b)	(c)	(d)
ax of sym	$x = 1$	$x = 3$	$x = 4$	$x = 2.5$
vertex	$(2, -1)$	$(3, -1)$	$(4, 28)$	$(2.5, -12)$
domain	$\{x x \in \mathbb{R}\}$			
range	$\{y y \geq -1, y \in \mathbb{R}\}$	$\{y y \leq -1, y \in \mathbb{R}\}$	$\{y y \leq 28, y \in \mathbb{R}\}$	$\{y y \geq 12, y \in \mathbb{R}\}$

5. a) $f(x) = x^2 - 5x - 6$ graph 4d because it has a y -intercept of -6

b) $f(x) = -x^2 + 8x + 12$ graph 4b because it has a y -intercept of 12

c) $f(x) = -x^2 + 6x - 10$ graph 4c because it has a y -intercept of -10

d) $f(x) = x^2 - 4x + 3$ graph 4a because it has a y -intercept of 3

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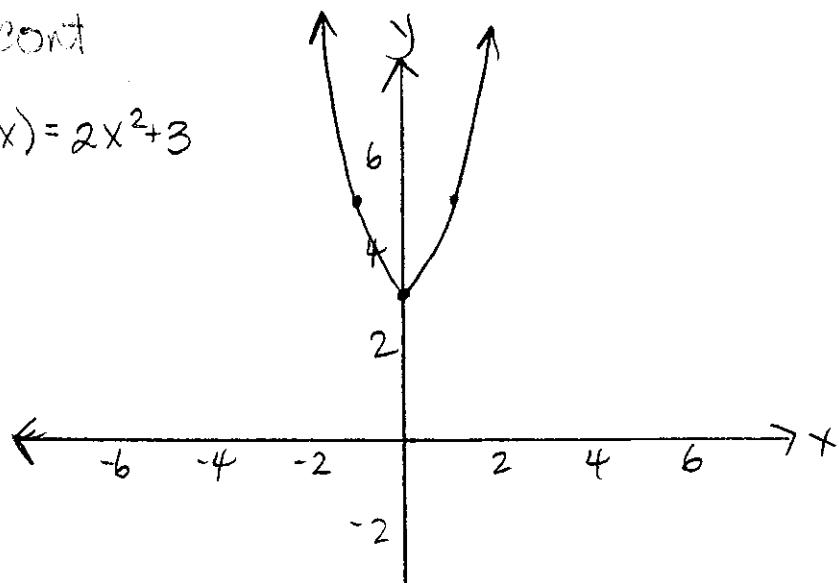
- 6. a) opens down so there is a maximum
y-value of vertex is 4 so that is the maximum
- b) opens up so there is a minimum
y-value of vertex is -3 so that is the minimum
- c) opens down so there is a maximum
y-value of vertex is 2 so that is the maximum

11. See graph paper

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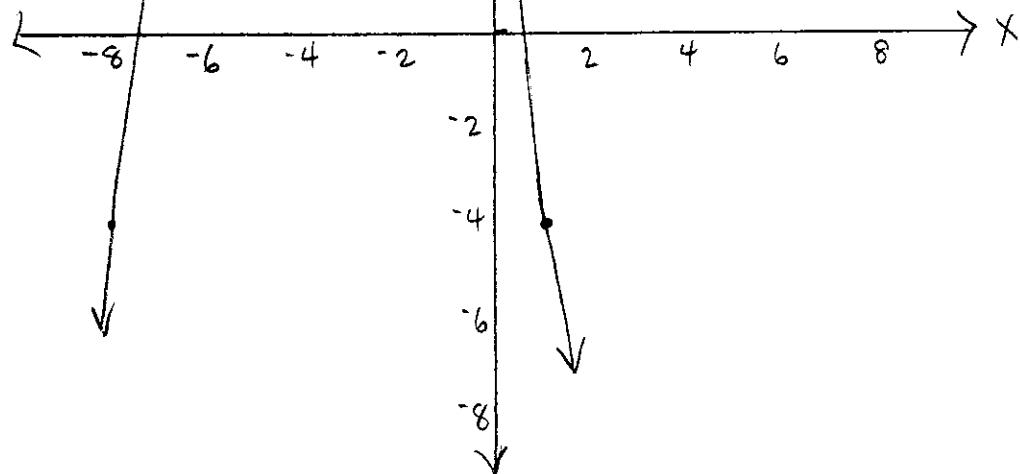
11. a) i) $f(x) = 2x^2 + 3$

x	y
0	3
1	5
2	11
-1	5
-2	11



b) ii) $f(x) = -x^2 - 7x + 4$

x	y
0	4
1	-4
2	-14
-1	10
-2	14
-3	16
-4	16
-5	14



Finish the rest using symmetry.